

Grade 12

Mathematics P2-MEMO
September 2020

MARKS: 150
TIME: 3 hours

NOTE:

- If a candidate answers a question TWICE, only mark the FIRST attempt.
- If a candidate has crossed out an attempt of a question and not redone the question, mark the crossed out version.
- Consistent accuracy applies in ALL aspects of the marking guidelines.
Stop marking at the second calculation error.
- Assuming answers/values in order to solve a problem is NOT acceptable.

NOTA:

- As 'n kandidaat 'n vraag TWEE KEER beantwoord, merk slegs die EERSTE poging.
- As 'n kandidaat 'n antwoord van 'n vraag doodtrek en nie oordoen nie, merk die doodgetrekte poging.
- Volgehoue akkuraatheid word in ALLE aspekte van die nasienriglyne toegepas.
Hou op nasien by die tweede berekeningsfout.
- Aanvaar van antwoorde/waardes om 'n probleem op te los, word NIE toegelaat nie.

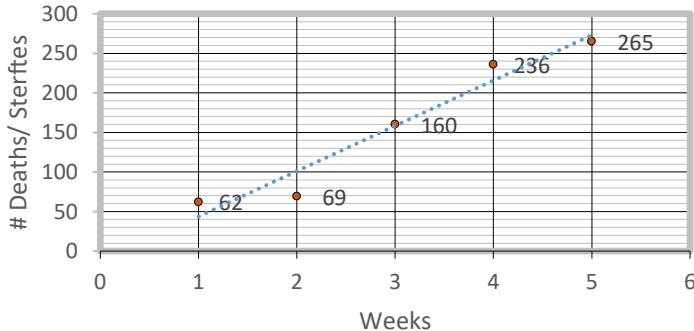
GEOMETRY / MEETKUNDE:

S	A mark for a correct statement (a statement mark is independent of a reason)
	<i>'n Punt vir 'n korrekte bewering. ('n Punt vir 'n bewering is onafhanklik van die rede.)</i>
R	A mark for a correct reason . (a reason mark may only be awarded if the statement is correct.)
	<i>'n Punt vir 'n korrekte rede. ('n Punt word slegs vir 'n rede toegeken as die bewering korrek is.)</i>
S&R	Award a mark if the statement AND reason are both correct.
	<i>Ken 'n punt toe as beide die bewering EN rede korrek is.</i>

QUESTION/ VRAAG 1

#	Suggested answer(s)/ Voorgestelde antwoord(e)	Descriptors/ Beskrywers	Mark/ Punt										
Recover/ Herstel  <table><tr><td>8</td><td>39</td><td>63</td><td>69</td><td>104</td><td>141</td><td>183</td><td>191</td><td>301</td><td>592</td></tr></table> Source/ Bron: https://www.worldometers.info/coronavirus/?utm_campaign=homeAdvegas1?#countries				8	39	63	69	104	141	183	191	301	592
8	39	63	69	104	141	183	191	301	592				
1.1	Standard deviation/ Standaardafwyking = 163,13	✓ ✓ Answer/Antwoord	(2) K										
1.2	Mean/ Gemiddelde: 169,1 (5,97; 332.23) Thus/ Dus: 9 countries/ Lande	✓ Mean/ Gemiddelde ✓ Boundaries/ Eindpunte ✓ Answer/Antwoord	(3) R										
1.3	False; The infection rate could have been higher./ Virus was probably detected earlier there/ Vals; Die infeksiekoers kon hoër wees/ Virus was waarskynlik daar gevind : True; better medical facilities/ Earlier detection lead to earlier safety precautions, etc/ Waar; Better facilities; medical facilities/ Earlier waarneming lei tot vroeër veiligheidsmaatreels, ens	✓ Selection/ Keuse ✓ Reason/ Rede Reason must justify TRUE/ FALSE 2 or 0	(2) P										
1.4	Sum/ Som: 1691 New mean/ Nuwe gemidd: $209.72 \times 11 = 2306.92$ $2306.92 - 1691 = 616$ cases/ gevalle	✓ New Total/ Nuwe Totaal ✓ Answer/Antwoord	(2) C										
			[9]										

QUESTION/ VRAAG 2

#	Suggested answer(s)/ Voorgestelde antwoord(e)	Descriptors/ Beskrywers	Mark/ Punt												
	<table><tr><td>Week</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td></tr><tr><td>No of Deaths/ Getal sterftes</td><td>62</td><td>69</td><td>160</td><td>236</td><td>265</td></tr></table> Source/ Bron: https://www.worldometers.info/coronavirus/country/south-africa/	Week	1	2	3	4	5	No of Deaths/ Getal sterftes	62	69	160	236	265		
Week	1	2	3	4	5										
No of Deaths/ Getal sterftes	62	69	160	236	265										
2.1	Covid-19 deaths/ sterftes (per week) 	✓ Correct axes/ Korrekte asse ✓ Plotting of points/ Afstip van punte	(2)												

Memo

2.2	$A = -13,5; B = 57,3$ $y = -13,5 + 57,3x$	✓ A and/ en B ✓ equation/ vergelyking	(2)	R
2.3	Graph/ Grafiek	✓ + gradient/ gradient; ✓ through/ deur ≈ 160	(2)	K
2.4	$r = 0,97$; Strong positive relation/ Sterk positiewe verwantskap	✓ Value of/ Waarde van r ; ✓ strong positive/ sterk positiewe	(2)	K
2.5	Humankind would be totally wiped out/ A cure would be found sooner or later/ People practice safety measures/ Mense sal dan totaal uitgewis wees/ 'n Entstof sal een of ander tyd gevind word/ mense pas veiligheidmaatreëls toe.	✓ Answer/ Antwoord	(1)	P
2.6	$y = -13,5 + 57,3(12)$ ≈ 674	✓ Subst 12 in eq/ vervang 12 in vgl ✓ Answer/ Antwoord -1 if decimal is stated;	(2)	R
2.7	Reaching its peak by this week OR number of deaths increased drastically over the last few weeks OR the least squares regression model is just an estimation of this situation/ Bereik sy piek teen hierdie week OF aantal sterftes het drasties toegeneem tydens die vorige paar weke OF die kleinste-kwadrate regressiemodel is slegs 'n benadering van die situasie.	✓ Valid reason/ Geldige rede	(1)	P
			[12]	

QUESTION/ VRAAG 3

#	Suggested answer(s)/ Voorgestelde antwoord(e)	Descriptors/ Beskrywers	Mark/ Punt
3.1.1	$EF = \sqrt{(-2-4)^2 + (-1-2)^2}$ $= \sqrt{45} \quad [= 3\sqrt{5} = 6,71]$	✓ subst/ vervang in EF ✓ Answer/ Antwoord	(2) K
3.1.2	$m_{DH} = \tan D\hat{H}O$ $= \tan 45^\circ$ $= 1$	✓ $m_{DH} = \tan 45^\circ$ AO = no marks/ geen punte	(1) K
3.1.3	$m_{DE} = \frac{d - (-1)}{2 - (-2)} = 1$ $\frac{d+1}{4} = 1$ $d+1 = 4$ $\therefore d = 3$	✓ subst/ vervang m_{DE} ✓ simplify/ vereenvoudig AO = no marks/ geen punte	(2) R
3.1.4	$GF \parallel DE \therefore m_{GF} = m_{DE} = 1$ $\therefore y = x + c$ (4; 2): $2 = 4 + c$ $c = -2$ $\therefore y = x - 2$	✓ $m_{GF} = 1$ ✓ subst/ vervang $F(4; 2)$ ✓ Answer/ Antwoord	(3) R
3.1.5	G(8; 6)	✓ x; ✓ y	(2) R
3.1.6	$ED = \sqrt{(-2-2)^2 + (-1-3)^2}$ $= \sqrt{32}$ $\frac{EF}{ED} = \frac{\sqrt{45}}{\sqrt{32}}$ $= \frac{3\sqrt{5}}{4\sqrt{2}} \times \frac{\sqrt{2}}{\sqrt{2}} = \frac{3\sqrt{10}}{8}$	✓ subst/ vervang in ED ✓ Answer/ Antwoord ✓ $\frac{EF}{ED}$ ✓ $\times \frac{\sqrt{2}}{\sqrt{2}}$	(4) C

3.1.7	$x^2 + y^2 = 45$	✓ x^2 ; ✓ y^2 or centre (0; 0) ✓ 45	(3)	C
3.2.1	AD x -axis/ as $\therefore \tan \theta = \frac{3}{2}$ $\theta = 56,31^\circ$	✓ $\tan \theta = \frac{3}{2}$ ✓ Answer/ Antwoord	(2)	R
3.2.2	Let A be the point/ Laat A die punt $(x; \frac{3}{2}x)$ wees $\therefore D(5; \frac{3}{2}x)$ $AD^2 = DC^2$ OR $AD = DC$ $(5-x)^2 = (\frac{3}{2}x)^2$ $5-x = \frac{3}{2}x$ $25 - 10x + x^2 = \frac{9}{4}x^2$ $10 - 2x = 3x$ $4x^2 - 40x + 100 = 9x^2$ $10 = 5x \Rightarrow x = 2$ $0 = 5x^2 + 40x - 100$ $= x^2 + 8x - 20$ $= (x-2)(x+10)$ $\therefore x = 2$ $\therefore A(2; 3)$	✓ method/ metode ✓ equate lengths/ stel lengtes = ✓ standard form/ standaardv ✓ x ✓ y	(5)	P
			[24]	

QUESTION/ VRAAG 4

#	Suggested answer(s)/ Voorgestelde antwoord(e)	Descriptors/ Beskrywers	Mark/ Punt
4.1	$x^2 - 10x + y^2 + 6y - 2 = 0$ $(x^2 - 10x + 25) + (y^2 + 6y + 9) = 2 + 25 + 9$ $(x-5)^2 + (y+3)^2 = 36$ Centre/ Middelpt (5; -3)	✓ LHS/ LK: +25 + 9 ✓ RHS/ RK: +25 + 9 ✓ equation/ vergelyking ✓ x ; ✓ y	(5) R
4.2.1	$G(0; \frac{8}{5})$	✓ x ✓ y	(2) K
4.2.2	Area/ Oppervlakte = $\frac{1}{2} \times EF \times OG$ $= \frac{1}{2} \times 2 \left(\frac{8}{5}\right) \times \frac{8}{5}$ $= \frac{64}{25} \text{ units}^2 / \text{eenhede}^2$	✓ substitute/ vervanging ✓ Answer/ Antwoord	(2) R
4.2.3	$m_{MA} = \frac{2}{5}$ [radius $\perp$ tangent/ raaklyn] $\therefore y = \frac{2}{5}x + c$ $\therefore y = \frac{2}{5}x - 4$	✓ $m = \frac{2}{5}$ ✓ equation/ vergelyking	(2) R

4.2.4	$-3 = \frac{2}{5}a - 4 \quad \text{OR} \quad m_{rad} = \frac{-3 - (-4)}{a - 0} = \frac{2}{5} = \frac{1}{a}$ $\therefore a = 2\frac{1}{2}$ $r^2 = \left(2\frac{1}{2} - 0\right)^2 + (-3 + 4)^2 \quad \text{OR} \quad \left(2\frac{1}{2} - 5\right)^2 + (-3 + 2)^2$ $= 7,25$ $\therefore \left(x - 2\frac{1}{2}\right)^2 + (y + 3)^2 = 7,25$ OR/ OF $MA^2 = MB^2$ $a^2 + (-3 + 4)^2 = (a - 5)^2 + (-3 + 2)^2$ $a^2 + 1 = a^2 - 10a + 25 + 1$ $10a = 25$ $a = 2\frac{1}{2}$ $\therefore r^2 = \left(2\frac{1}{2}\right)^2 + 1$ $= 7,25$ $\therefore \left(x - 2\frac{1}{2}\right)^2 + (y + 3)^2 = 7,25$	✓ substitute/ vervanging ✓ a ✓ r^2 ✓ equation/ vergelyking ✓ substitute/ vervanging ✓ a ✓ r^2 ✓ equation/ vergelyking	(4)	
			(4)	C
			[15]	

QUESTION/ VRAAG 5

#	Suggested answer(s)/ Voorgestelde antwoord(e)	Descriptors/ Beskrywers	Mark/ Punt
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5.1	$\sin(90^\circ + x) \cdot \cos(-x) - \cos(180^\circ - x) \tan(x - 180^\circ) \cdot \sin(x)$ $= \cos x \cos x - (-\cos x)(\tan x)(\sin x)$ $= \cos^2 x - (-\cos x) \left(\frac{\sin x}{\cos x}\right) \sin x$ $= \cos^2 x + \sin^2 x$ $= 1$	✓ ✓ $\cos x$; $\cos x$ ✓ $-\cos x$ ✓ $\frac{\sin x}{\cos x}$ or $\tan x$ ✓ Answer/ Antwoord	(5)	R
5.2.1	$\sin 56^\circ = \sin(42 + 14) = \sin 42^\circ \cdot \cos 14^\circ + \cos 42^\circ \cdot \sin 14^\circ$ $= a + b$	✓ Expand/ Uitbrei ✓ Answer/ Antwoord	(2)	C
5.2.2	$\sin 28^\circ = \sin(42 - 14) = \sin 42^\circ \cdot \cos 14^\circ - \cos 42^\circ \cdot \sin 14^\circ$ $= a - b$	✓ Expand/ Uitbrei ✓ Answer/ Antwoord	(2)	C
5.2.3	$\cos 56^\circ$ $= \cos(2 \times 28^\circ)$ $= 1 - 2\sin^2 28^\circ$ $= 1 - 2(a - b)^2$ $= 1 - 2(a^2 - 2ab + b^2)$ $= 1 - 2a^2 + 4ab - 2b^2$	✓ $\cos(2 \times 28^\circ)$ ✓ Expansion/ Uitbreiding ✓ Substitute/ Vervang $(a - b)$	(3)	C

Memo

5.3.1	$\frac{\cos 2\theta + \sin^2 \theta}{1 + \sin \theta} = 1 - \sin \theta$ $LHS = \frac{\cos^2 \theta - \sin^2 \theta + \sin^2 \theta}{1 + \sin \theta}$ $= \frac{\cos^2 \theta}{1 + \sin \theta}$ $= \frac{1 + \sin \theta}{1 - \sin^2 \theta}$ $= \frac{1 + \sin \theta}{(1 - \sin \theta)(1 + \sin \theta)}$ $= \frac{1 + \sin \theta}{1 + \sin \theta} = 1 - \sin \theta = RHS$	$\checkmark \cos^2 \theta - \sin^2 \theta$ $\checkmark$ Simplify/ Vereenvoudig $\checkmark \cos^2 \theta = 1 - \sin^2 \theta$ $\checkmark$ Factorise/ Faktoreiseer	(4)	C
5.3.2	$\sin \theta = -1$ $\theta = 270^\circ + k \cdot 360^\circ$ for / vir $k \in \mathbb{Z}$	$\checkmark$ equation/ vergelyking $\checkmark$ Answer/ Antwoord	(2)	R
5.4	$(\cos \theta + 2)^2 + (\sin \theta - 1)^2 = (\sqrt{6})^2$ $\cos^2 \theta + 4 \cos \theta + 4 + \sin^2 \theta - 2 \sin \theta + 1 = 6$ $1 + 4 \cos \theta - 2 \sin \theta + 5 = 6$ $-2 \sin \theta = -4 \cos \theta$ $\frac{\sin \theta}{\cos \theta} = 2$ $\tan \theta = 2$	$\checkmark$ Substitution/ vervanging $\checkmark$ Simplify/ Vereenvoudig $\checkmark$ Answer/ Antwoord	(3)	P
			[21]	

QUESTION/ VRAAG 6

#	Suggested answer(s)/ Voorgestelde antwoord(e)	Descriptors/ Beskrywers	Mark /Punt
6.1	$\sin x = \cos 2x - 1$ $\sin x = 1 - 2 \sin^2 x - 1$ $2 \sin^2 x + \sin x = 0$ $\sin x (2 \sin x + 1) = 0$ $\sin x = 0$ or/ of $\sin x = -\frac{1}{2}$ $x = 0^\circ + k \cdot 360^\circ$ OR $x = 210^\circ + k \cdot 360^\circ$ $x = 180^\circ + k \cdot 360^\circ$ $x = 330^\circ + k \cdot 360^\circ$ / $-30^\circ + k \cdot 360^\circ$ $\therefore x = -180^\circ; -150^\circ; -30^\circ; 0^\circ$	$\checkmark 1 - 2 \sin^2 x$ $\checkmark$ Standard form/ Standaardvorm $\checkmark \sin x = 0$ or $\sin x = -\frac{1}{2}$ $\checkmark \checkmark$ General solution/ Algemene Oplossing [1 from each group/ block] $\checkmark$ Answer/ Antwoord	(6) C

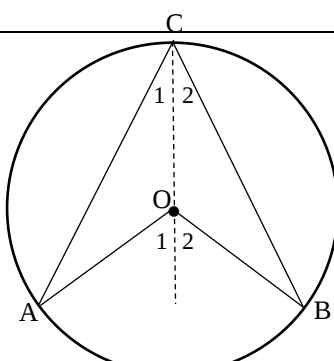
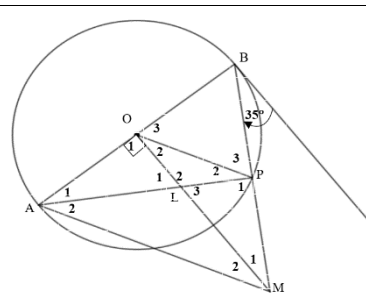
Memo

6.2.1		✓ x-intercept/ afsnit $(-90^\circ; 0)$ ✓ $(-180^\circ; 1)$ and/ en $(0; 1)$	(2)	R
6.2.2	$h(x) = -\sin x - 1$	✓ Answer/ Antwoord	(1)	K
6.2.3	$-180^\circ \leq x \leq -90^\circ$	✓ endpoints/ eindpunte ✓ inequality notation/ ongelykheidsnotasie	(2)	P
				[11]

QUESTION/ VRAAG 7

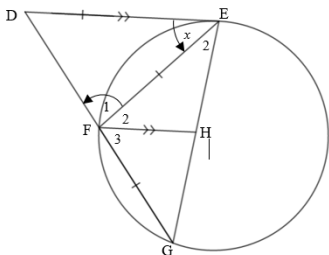
#	Suggested answer(s)/ Voorgestelde antwoord(e)	Descriptors/ Beskrywers	Mark/ Punt	
7.1	$\cos(90^\circ - x) = \frac{PA}{3}$ $\sin x = \frac{PA}{3}$ $PA = 3 \sin x$	 ✓ Reduction/ Reduksie – $\sin x$ ✓ Answer/ Antwoord	(2)	R
7.2	$In \Delta PAT: \frac{\sin(90^\circ + x)}{PT} = \frac{\sin 2x}{PA}$ $\frac{\cos x}{PT} = \frac{2 \sin x \cdot \cos x}{3 \sin x}$ $PT = \frac{3 \sin x \cos x}{2 \sin x \cos x}$ $= \frac{3}{2}$ Yes, they are 1,5m apart/ Ja, hulle is 1,5m van mekaar	 ✓ Subst / vervang in sin rule/ reël ✓ expansion/ uitbreiding: $\sin 2x$ ✓ Answer/ Antwoord ✓ Conclusion/ Afleiding	(4)	C
7.3	$\therefore \widehat{APT} = 30^\circ$ $Area/Oppervlakte \Delta PAT = \frac{1}{2} (PA)(PT) \sin 30^\circ$ $= \frac{1}{2} (3 \sin 20^\circ) \left(\frac{3}{2}\right) \left(\frac{1}{2}\right)$ $= 0,38 m^2$	 ✓ $\widehat{APT}$ ✓ Subst/ Vervang in Area rule/ reël ✓ Answer/ Antwoord	(3)	R
			[9]	

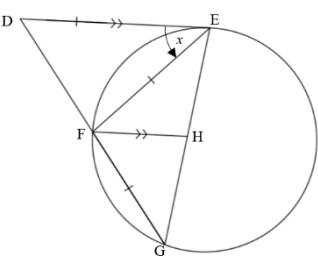
QUESTION/ VRAAG 8

#	Suggested answer(s)/ Voorgestelde antwoord(e)		Descriptors/ Beskrywers	Mark/ Punt	
8.1					
	Construction/ Konstruksie: Draw CO produced/ Trek CO verleng Proof/ bewys: $\hat{C}_1 = \hat{A}$ [$\angle$ s opposite = sides/ $\angle$ e teenoor = sye] $\therefore \hat{O}_1 = 2\hat{C}_1$ [ext. $\angle$ of Δ / buite $\angle$ van Δ] Similarly/ Netso: $\hat{O}_2 = 2\hat{C}_2$ Now/ Nou: $\hat{O}_1 + \hat{O}_2 = 2\hat{C}_1 + 2\hat{C}_2$ $\therefore \hat{AOB} = 2(\hat{C}_1 + \hat{C}_2)$ $= 2\hat{ACB}$		✓ Construction/ Konstruksie ✓ S/ R ✓ S/ R ✓ S (Similarly/ Netso) ✓ S (any/ enige 1)	(5)	K
8.2					
8.2.1	(a)	$\hat{A}_1 = 35^\circ$ [tan- chord thm/ raakl-koordstelling]	✓ S ✓ R	(2)	K
	(b)	$\hat{O}_3 = 70^\circ$ [$\angle$ at centre = 2 $\angle$ at circumf/ middelpts $\angle$ = 2 omtr. $\angle$]	✓ S ✓ R	(2)	K
	(c)	$\hat{P}_3 = 55^\circ$ [$\sum$ interior/ binne $\angle$ of/ van (isosceles/gelykbenige) Δ]	✓ S ✓ R	(2)	K
	(d)	$\hat{BOM} = 90^\circ$ [adjacent/ aanligg – suppl.] And/ en $\hat{OBM} = 55^\circ$ [$\sum \angle$ s of/ van (isosceles/gelykbenige) Δ] OR/ OF [$\angle$ s opposite = radii/ sides/ $\angle$ e teenoor = radiusse/ sye] OR/OF $\hat{OBS} = 90^\circ$ [tan/ raakl. $\perp$ radius] $\therefore \hat{M}_1 = 35^\circ$ [$\sum \angle$ s of/ van Δ] OR/OF $\hat{APB} = 90^\circ$ [$\angle$ in semi circle/ $\angle$ in halwe sirkel] $\therefore \hat{P}_1 = 90^\circ$ [adj./ aanligg./ suppl] $= \hat{O}_1$ AMPO is cycl quad/ is 'n kvh [conv. $\angle$ s Subt by same chord/ omg. $\angle$ e ondersp. deur selfde koord] $\therefore \hat{M}_1 = \hat{A}_1 = 35^\circ$ [$\angle$ s Subt by same chord/ $\angle$ e ondersp. deur selfde koord]	✓ S/ R ✓ S/ R ✓ S	(3)	K
8.2.2	(a)	$\hat{APB} = 90^\circ$ [$\angle$ in semi-circle/ $\angle$ in halwe sirkel] $= \hat{O}_1$ [Given/ Gegee] $\therefore$ OLPB is a cycl. quad/ is 'n kvh [ext $\angle$ =opp. int $\angle$ / buite $\angle$ =teenoorst. binne $\angle$]	✓ S ✓ R ✓ R	(3)	R

	(b)	$\widehat{OBS} = 90^\circ$ [tan/ raakl. $\perp$ radius] $= \widehat{O_1}$ [Given/ Gegee] $\therefore BS \parallel OM$ [corresp. $\angle$ s =/ ooreenk. $\angle$ e =] OR/ OF	✓ S/ R	(2)	
		$\widehat{OBS} = 90^\circ$ [tan/ raakl.-radius] $= \widehat{BOM}$ [Proved/ Bewys] $\therefore BS \parallel OM$ [co-int. $\angle$ s suppl./ ko-binne $\angle$ e suppl.] OR/ OF	✓ R		
		$\widehat{M_1} = 35^\circ$ [Proved/ Bewys] $= \widehat{MBS}$ [Given/ Gegee] $\therefore BS \parallel OM$ [alt. $\angle$ s =/ verw. $\angle$ e =]	✓ S/ R ✓ R		
	(c)	$\widehat{P_2} = \widehat{A_1} = 35^\circ$ [$\angle$ s opposite = sides/radii/ $\angle$ e teenoor = sye/ radiusse] $= \widehat{M_1}$ $\therefore OP$ is a tangent to the circle through P, L and M [converse tan-chord thm/ omgekeerde raakl-koordstelling]	✓ S ✓ R ✓ R	(3)	R
					[22]

QUESTION/ VRAAG 9

#	Suggested answer(s)/ Voorgestelde antwoord(e)	Descriptors/ Beskrywers	Mark/ Punt
			
9.1	$\widehat{EFH} = x$ [alt. $\angle$ s; DE//FH/ verw. $\angle$ e; DE//FH] $\widehat{G} = x$ [tan- chord thm/ raakl-koordstelling] $\widehat{FEG} = \widehat{G} = x$ [$\angle$ s opposite = sides/ $\angle$ e teenoor = sye]	✓ S ✓ R ✓ S ✓ R ✓ S ✓ R	(6) K
9.2.1	$\frac{EH}{HG} = \frac{DF}{FG}$ [FH//DE or line // 1 side of Δ / lyn // 1 sy van Δ] $= \frac{DF}{DE}$ [FG = DE; given/ Gegee] $= y$	✓ S ✓ R ✓ S	(3) R
9.2.2	In $\triangle DEF$: $\widehat{D} = \frac{180^\circ - x}{2}$ [$\sum \angle$ s of/ van (isosceles/gelykbenige) Δ] In $\triangle DEG$: $\widehat{D} = 180^\circ - 3x$ [$\sum \angle$ s of/ van Δ] $\therefore \frac{180^\circ - x}{2} = 180^\circ - 3x$ $\therefore 180^\circ - x = 360^\circ - 6x$ $\therefore 5x = 180^\circ$ $\therefore x = 36^\circ$ $\therefore \widehat{D} = \frac{180^\circ - 36^\circ}{2} = 72^\circ$	✓ S ✓ R ✓ S ✓ (equating/ gelyk stel) ✓ Simplify/ Vereenvoudig ✓ value of/ waarde van x	(5) C

9.2.3	<u>In $\triangle DGE$ and/ en $\triangle DEF$:</u> $\widehat{D}$ is common/ <i>gemeen</i> $\widehat{G} = \widehat{DEF} = x$ [proved/ <i>bewys</i>] $\therefore \widehat{DEG} = \widehat{DFE}$ [3^{rd}/ 3^{de} $\angle$] $\therefore \triangle DGE \parallel \triangle DEF$ [$\angle, \angle, \angle$]	✓ S ✓ S ✓ S OR/ OF ✓ R ($\angle, \angle, \angle$) (Can also work with 72° etc)	(3)	R
9.2.4	$\therefore \frac{DG}{DE} = \frac{GE}{EF} = \frac{DE}{DF}$ from/ <i>vanaf</i> 9.2.3 OR/ OF $\triangle DGE \parallel \triangle DEF$ $\Rightarrow DE^2 = DF \cdot DG$	✓ S ✓ R Can only give needed 2 ratios	(2)	K
9.2.5	$\frac{DE}{DF} = \frac{DG}{DE}$ $\frac{1}{y} = \frac{DF+FG}{DE}$ $= \frac{DF}{DE} + \frac{FG}{DE}$ $= y + 1$ $\therefore y^2 + y = 1$	✓ S Correct Proportion/ <i>Korrekte Eweredigheid</i> ✓ $\frac{DE}{DF} = \frac{1}{y}$ ✓ $\frac{DG}{DE} = \frac{DF+FG}{DE}$ ✓ $\frac{1}{y} = \frac{DF}{DE} + \frac{FG}{DE}$ ✓ $\frac{FG}{DE} = 1$	(5)	P
9.2.6	In $\triangle DEF$: $EF^2 = DF^2 + DE^2 - 2 DF \cdot DE \cdot \cos D$ $\therefore \cos D = \frac{DF^2 + DE^2 - EF^2}{2 DF \cdot DE}$ $= \frac{DF^2}{2 DF \cdot DE} = \frac{DF}{2 DE}$ $\therefore \cos 72^\circ = \frac{1}{2} y$ 	✓ cos rule/ <i>reël</i> for/ <i>vir</i> $\triangle DEF$ ✓ $DE^2 - EF^2 = 0$ ✓ Simplify/ <i>Vereenvoudig</i>	(3)	P
				[27]
TOTAL/ TOTAAL				150