



education
MPUMALANGA PROVINCE
REPUBLIC OF SOUTH AFRICA

**NATIONAL
SENIOR CERTIFICATE**

GRADE 12

MATHEMATICS PAPER 2

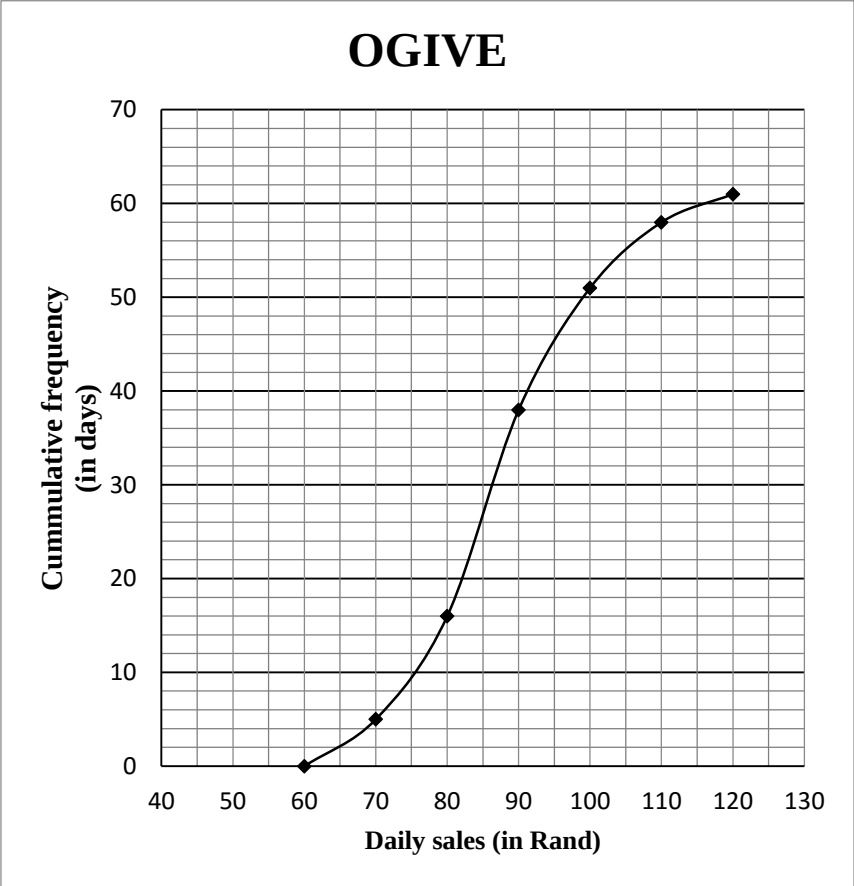
September 2019

MARKING GUIDELINES

MARKS: 150

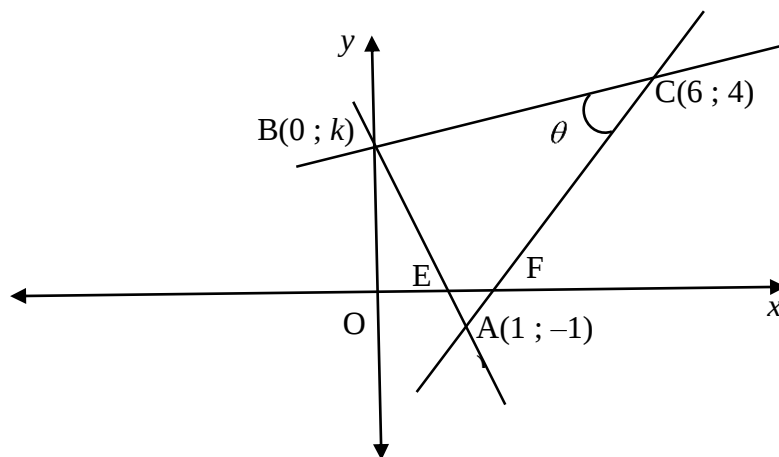
This marking guidelines consist of 23 pages

Question 1

1.1	<table border="1"> <thead> <tr> <th>Interval</th><th>Frequency</th><th>Cummulative frequency</th></tr> </thead> <tbody> <tr> <td>$60 < x \leq 70$</td><td>5</td><td>5</td></tr> <tr> <td>$70 < x \leq 80$</td><td>11</td><td>16</td></tr> <tr> <td>$80 < x \leq 90$</td><td>22</td><td>38</td></tr> <tr> <td>$90 < x \leq 100$</td><td>13</td><td>51</td></tr> <tr> <td>$100 < x \leq 110$</td><td>7</td><td>58</td></tr> <tr> <td>$110 < x \leq 120$</td><td>3</td><td>61</td></tr> </tbody> </table>	Interval	Frequency	Cummulative frequency	$60 < x \leq 70$	5	5	$70 < x \leq 80$	11	16	$80 < x \leq 90$	22	38	$90 < x \leq 100$	13	51	$100 < x \leq 110$	7	58	$110 < x \leq 120$	3	61	✓ frequency ✓✓ accumulative frequency (3)
Interval	Frequency	Cummulative frequency																					
$60 < x \leq 70$	5	5																					
$70 < x \leq 80$	11	16																					
$80 < x \leq 90$	22	38																					
$90 < x \leq 100$	13	51																					
$100 < x \leq 110$	7	58																					
$110 < x \leq 120$	3	61																					
1.2	OGIVE 	✓ angle point ✓ use of cumulative frequency ✓ upper limits ✓ free hand curve (4)																					
1.3	$61 - 51 = 10$	✓✓ answer (2)																					
1.4	Medium = 87 (between 85 and 88)	✓✓ answer (2)																					
		[11]																					

QUESTION 2

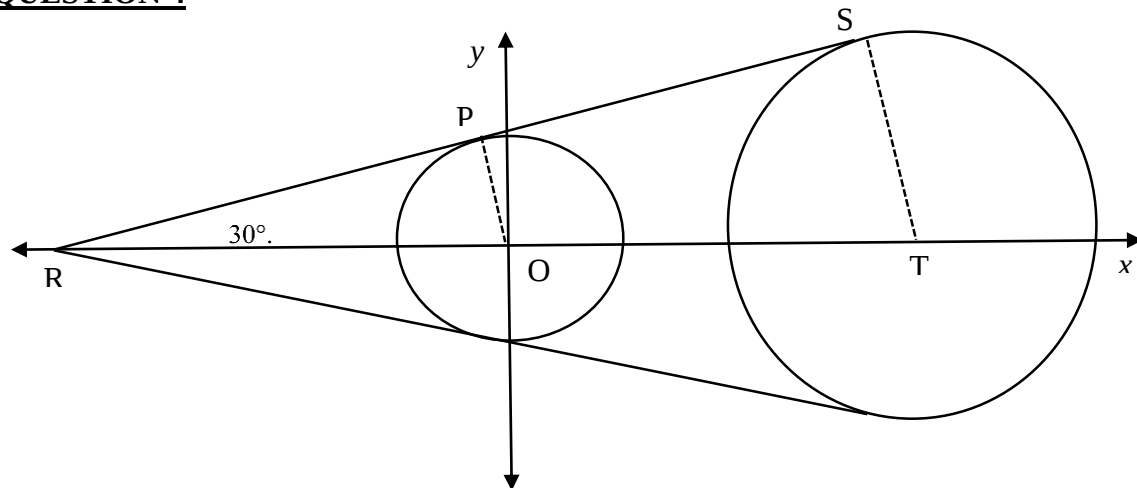
2.1.1	By using a calculator : $a = 76,60$ (76,59564211) $b = 0,1(0.09544928654)$ $\therefore$ equation of line of least squares is $y = 76,60 + 0,10x$	✓ a ✓ b ✓ equation (3)
2.1.2	$y = 76,60 + 0,10(57)$ ≈ 82	✓ substitution ✓ answer (2)
2.1.3	$r = 0,1408374211$ $r \approx 0,14$	✓✓ $r \approx 0,14$ (1)
2.1.4	r value is low which means that the data is spread around the regression line. Therefore prediction using the regression line will be invalid .	✓ invalid (1)
2.2.1	22	✓ 22 (1)
2.2.2	$\frac{1320}{22} = 60$	✓ $\frac{1320}{22}$ ✓ 60 (2)
		[10]

QUESTION 3

3.1	$AB : y + 3x - 2 = 0$ $\therefore y = -3x + 2$ $\therefore k = 2$	$\checkmark y = -3x + 2$ $\checkmark k = 2$ (2)
3.2	$AC = \sqrt{(1-6)^2 + (-1-4)^2}$ $= \sqrt{50}$ $= 5\sqrt{2}$	$\checkmark$ substitution $\checkmark$ answer (2)
3.3	$m_{AB} = \frac{-1-2}{1-0} = -3$ $m_{BC} = \frac{4-2}{6-0} = \frac{1}{3}$ $m_{AB} \times m_{BC} = -3 \times \frac{1}{3} = -1$ $\therefore \hat{ABC} = 90^\circ.$	$\checkmark m_{AB} = -3$ $\checkmark m_{BC} = \frac{1}{3}$ $\checkmark m_{AB} \times m_{BC} = -1$ (3)
3.4	$\tan \beta = m_{AC} = 1$ $\beta = 45^\circ$ $\tan \phi = m_{BC} = \frac{1}{3}$ $\phi = 18,43^\circ$ $\theta = 45^\circ - 18,43^\circ$ [ext $\angle$ of Δ] $= 26,57^\circ$ OR	$\checkmark \tan \beta = m_{AC} = 1$ $\checkmark \beta$ $\checkmark \phi$ $\checkmark$ method $\checkmark$ answer (5)

$AC = \sqrt{(1-6)^2 + (-1-4)^2}$ $= \sqrt{50}$ $= 5\sqrt{2}$ $AB = \sqrt{(0-1)^2 + (2+1)^2}$ $= \sqrt{10}$ $\sin \theta = \frac{AB}{AC}$ $= \frac{\sqrt{10}}{5\sqrt{2}}$ $= \frac{\sqrt{5}}{2}$ $\therefore \theta = 26.57^\circ$ OR $\frac{\sin \theta}{AB} = \frac{\sin B}{AC}$ $\sin \theta = \frac{\sqrt{10} \sin 90^\circ}{5\sqrt{2}}$ $= \frac{\sqrt{5}}{5}$ $\therefore \theta = 26.57^\circ$	$\checkmark AC = 5\sqrt{2}$ $\checkmark AB = \sqrt{10}$ $\checkmark \sin \theta = \frac{AB}{AC}$ $\checkmark \sin \theta = \frac{\sqrt{10}}{5\sqrt{2}}$ $\checkmark \text{ answer}$ (5) $\checkmark \frac{\sin \theta}{AB} = \frac{\sin B}{AC}$ $\checkmark AC = 5\sqrt{2}$ $\checkmark AB = \sqrt{10}$ $\checkmark \sin \theta = \frac{\sqrt{10} \sin 90^\circ}{5\sqrt{2}}$ $\checkmark \text{ answer}$ (5)
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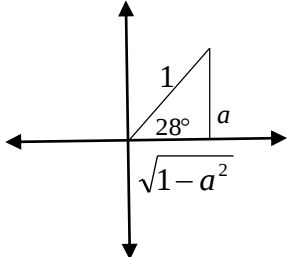
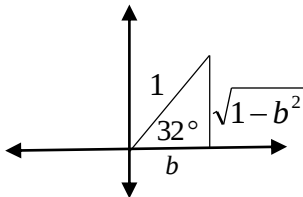
3.5	$\hat{BDC} = 90^\circ$ altitude $\therefore BC$ is the diameter (line subtends $90^\circ \angle$) midpoint of $BC : \left(\frac{0+6}{2}; \frac{2+4}{2} \right)$ $= (3;3)$ $(x-3)^2 + (y-3)^2 = r^2$ subst $B(0;2)$ $(0-3)^2 + (2-3)^2 = r^2$ $\therefore r^2 = 10$ $(x-3)^2 + (y-3)^2 = 10$ OR $\hat{BDC} = 90^\circ$ altitude $\therefore BC$ is the diameter (line subtends $90^\circ \angle$) midpoint of $BC : \left(\frac{0+6}{2}; \frac{2+4}{2} \right)$ $= (3;3)$ $(x-3)^2 + (y-3)^2 = r^2$ subst $B(0;2)$ $(0-3)^2 + (2-3)^2 = r^2$ $\therefore r^2 = 10$ $(x-3)^2 + (y-3)^2 = 10$	✓ BC is diameter ✓ $(3;3)$ ✓ Substitution of $(0;2)$ ✓ equation (4) ✓ BC is diameter ✓ $(3;3)$ ✓ Substitution of $(0;2)$ ✓ equation (4)
3.6	$M_{AC} = \left(\frac{1+6}{2}; \frac{2+1}{2} \right)$ $= \left(\frac{7}{2}; \frac{3}{2} \right)$ $\frac{7}{2} = \frac{x+0}{2}$ $x = 7$ $D(7;1)$ $\frac{3}{2} = \frac{2+y}{2}$ $y = 1$	✓ $\frac{7}{2}$ ✓ $\frac{3}{2}$ ✓ $x = 7$ ✓ $y = 1$ (4)
		[20]

QUESTION 4

4.1	$T(6; 0)$	✓ $(6; 0)$ (1)
4.2	radius = 3	✓ radius = 3 (1)
4.3	$\tan 30^\circ = \frac{\sqrt{3}}{3}$ $0 = \frac{\sqrt{3}}{3}(-3) + c$ $c = \sqrt{3}$ $y = \frac{\sqrt{3}}{3}x + \sqrt{3}$	✓ $\tan 30^\circ = \frac{\sqrt{3}}{3}$ ✓ substitution ✓ $c = \sqrt{3}$ ✓ equation (4)
4.4	$y = -\frac{3}{\sqrt{3}}x + c$ radius $\perp$ tangent $0 = -\frac{3}{\sqrt{3}}(6) + c$ $c = \frac{18}{\sqrt{3}}$ $y = -\frac{3}{\sqrt{3}}x + \frac{18}{\sqrt{3}}$	✓ gradient ✓ $c = \frac{18}{\sqrt{3}}$ ✓ equation (3)

4.5	$\frac{\sqrt{3}}{3}x + \sqrt{3} = -\frac{3}{\sqrt{3}}x + \frac{18}{\sqrt{3}}$ $\frac{9x+54}{3\sqrt{3}} = +\frac{3x+9}{3\sqrt{3}}$ $12x = 45$ $x = \frac{15}{4} = 3\frac{3}{4}$ $y = \frac{\sqrt{3}}{3}\left(\frac{15}{4}\right) + \sqrt{3}$ $y = \left(\frac{9\sqrt{3}}{4}\right)$ $S\left(\frac{15}{4}; \frac{9\sqrt{3}}{4}\right)$	✓equating ✓simplification ✓x-value ✓substitution ✓y-value (5)
4.6	The distance between centres of circles: OT = 6 $r + R = 1 + 3$ $= 4$ The distance between the two circles = OT – (r + R) $= 6 - 4$ $= 2 \text{ units}$	✓ OT = 6 ✓ r + R = 1 + 3 ✓ 4 ✓ 2 (4)
		[18]

QUESTION 5

5.1	$\frac{\sin(A - 180^\circ) \cdot \tan(180^\circ - A) \cdot \cos A}{\cos(90^\circ + A)}$ $= \frac{\sin(-(180^\circ - A)) \cdot (-\tan A) \cdot \cos A}{-\sin A}$ $= \frac{-\sin A \cdot (-\tan A) \cdot \cos A}{-\sin A}$ $= -\frac{\sin A}{\cos A} \cdot \cos A$ $= -\sin A$	✓ $-\tan A$ ✓ $-\sin A$ ✓ $-\sin A$ ✓ identity ✓ answer (5)
5.2.1	 OR $\cos^2 28^\circ + \sin^2 28^\circ = 1$ $\cos^2 28^\circ + a^2 = 1$ $\cos^2 28^\circ = 1 - a^2$ $\cos 28^\circ = \sqrt{1 - a^2}$	✓ sketch ✓ answer (2) ✓ identity ✓ answer (2)
5.2.2	 $\cos 64^\circ$ $= \cos(2 \times 32^\circ)$ $= 2 \cos^2 32^\circ - 1$ $= 2b^2 - 1$ OR	✓ double angle ✓ answer (2)

	$\cos 64^\circ$ $= \cos(2 \times 32^\circ)$ $= 1 - 2 \sin^2 32^\circ$ $= 1 - 2(\sqrt{1-b^2})^2$ $= 1 - 2 + 2b^2$ $= 2b^2 - 1$ OR $\cos(2 \times 32^\circ)$ $= \cos^2 32^\circ - \sin^2 32^\circ$ $= b^2 - (\sqrt{1-b^2})^2$ $= b^2 - 1 + b^2$ $= 2b^2 - 1$	✓ double angle ✓ answer (2) ✓ double angle ✓ answer (2)
5.2.3	$\sin 4^\circ$ $= \sin(32^\circ - 28^\circ)$ $= \sin 32^\circ \cdot \cos 28^\circ - \cos 32^\circ \cdot \sin 28^\circ$ $= (\sqrt{1-b^2})(\sqrt{1-a^2}) - b \cdot a$ $= \sqrt{(1-b^2)(1-a^2)} - ab$	✓ compound $\angle$ ✓ expansion ✓ $\sqrt{1-b^2}$ ✓ $\sqrt{1-a^2}$ (4)
5.3	$\frac{1}{1-\sin x} - \frac{1}{1+\sin x} = \frac{2 \tan x}{\cos x}$ LHS: $\frac{1}{1-\sin x} - \frac{1}{1+\sin x} = \frac{1+\sin x - (1-\sin x)}{(1-\sin x)(1+\sin x)}$ $= \frac{1+\sin x - 1 + \sin x}{1-\sin^2 x}$ $= \frac{2 \sin x}{\cos^2 x}$ RHS: $\frac{2 \tan x}{\cos x} = \frac{2 \frac{\sin x}{\cos x}}{\cos x}$ $= \frac{2 \sin x}{\cos^2 x}$ $\therefore$ LHS = RHS	✓ LCD ✓ numerator ✓ $\frac{2 \sin x}{\cos^2 x}$ ✓ $\frac{\sin x}{\cos x}$ ✓ $\frac{2 \sin x}{\cos^2 x}$ (5)

	OR $\frac{1}{1 - \sin x} - \frac{1}{1 + \sin x} = \frac{2 \tan x}{\cos x}$ LHS: $\frac{1}{1 - \sin x} - \frac{1}{1 + \sin x} = \frac{1 + \sin x - (1 - \sin x)}{(1 - \sin x)(1 + \sin x)}$ $= \frac{1 + \sin x - 1 + \sin x}{1 - \sin^2 x}$ $= \frac{2 \sin x}{\cos^2 x}$ $= \frac{2 \sin x}{\cos x \cdot \cos x}$ $= \frac{2 \tan x}{\cos x}$ $\therefore \text{LHS} = \text{RHS}$	✓LCD ✓numerator ✓simplification ✓ $\frac{2 \sin x}{\cos^2 x}$ ✓ $\frac{\sin x}{\cos x} = \tan x$ (5)
		[18]

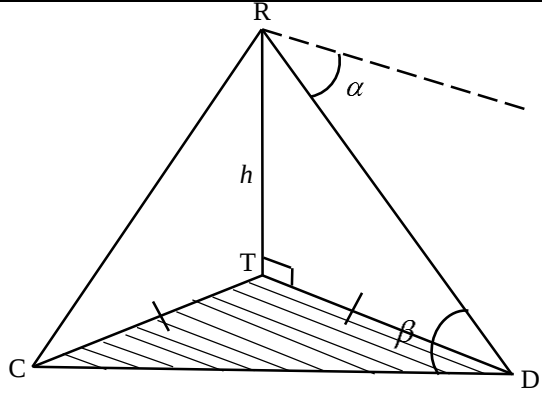
QUESTION 6**[16]**

6.1	$\sin(x + 60^\circ) = \cos \frac{1}{2}x$ $\sin(x + 60^\circ) = \sin\left(90^\circ - \frac{1}{2}x\right)$ <i>quadrant1:</i> $x + 60^\circ = 90^\circ - \frac{1}{2}x + 360.k, k \in \mathbb{Z}$ $x + \frac{1}{2}x = 30^\circ + 360.k$ $\frac{3}{2}x = 30^\circ + 360.k$ $x = 20^\circ + 240.k, k \in \mathbb{Z}$ <i>quadrant2:</i> $x + 60^\circ = 180^\circ - \left(90^\circ - \frac{1}{2}x\right) + 360.k, k \in \mathbb{Z}$ $x + 60^\circ = 180^\circ - 90^\circ + \frac{1}{2}x + 360.k$ $\frac{1}{2}x = 30^\circ + 360.k$ $x = 60^\circ + 720.k, k \in \mathbb{Z}$ $x \in \{20^\circ; 60^\circ; 260^\circ\}$ OR	✓ co-function ✓ 1st quad equation ✓ $x = 20^\circ + 240.k$ ✓ 2nd quad equation ✓ $x = 60^\circ + 720.k$ ✓✓ $x \in \{20^\circ; 60^\circ; 260^\circ\}$ (7)
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$\sin(x + 60^\circ) = \cos \frac{1}{2}x$ $\cos[90 - (x + 60^\circ)] = \cos \frac{1}{2}x$ <i>quadrant1</i> $[90 - (x + 60^\circ)] = \frac{1}{2}x + 360.k, k \in \mathbb{Z}$ $90 - x - 60^\circ = \frac{1}{2}x + 360.k$ $-\frac{3}{2}x = -30^\circ + 360.k$ $x = 20^\circ + 240.k, k \in \mathbb{Z}$ <i>quadrant4</i> $[90 - (x + 60^\circ)] = 360^\circ - \frac{1}{2}x + 360.k, k \in \mathbb{Z}$ $90 - x - 60^\circ = 360^\circ - \frac{1}{2}x + 360.k$ $30^\circ - x = 360^\circ - \frac{1}{2}x + 360.k$ $-\frac{1}{2}x = 330^\circ + 360.k$ $x = -660^\circ + 720.k$ $x \in \{20^\circ; 60^\circ; 260^\circ\}$	✓ co-function ✓ 1st quad equation ✓ $x = 20^\circ + 240.k$ ✓ 4th quad equation ✓ $x = -660^\circ + 720.k$ ✓✓ $x \in \{20^\circ; 60^\circ; 260^\circ\}$ (7)
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6.2.1		g: ✓ x – intercepts ✓ y – intercept ✓ turning points (3)
6.2.2	$20^\circ < x < 60^\circ$ or $260^\circ < x \leq 300^\circ$ OR $x \in (20^\circ; 60^\circ) \cup x \in (260^\circ; 300^\circ]$	✓ $20^\circ < x < 60^\circ$ ✓ $260^\circ < x \leq 300^\circ$ ✓ notation (3)
6.2.3	$120^\circ \leq x \leq 180^\circ$ $x = -60^\circ$ $x = 300^\circ$	✓✓ $120^\circ \leq x \leq 180^\circ$ ✓ $x = -60^\circ; 300^\circ$ (3)
		[16]

QUESTION 7

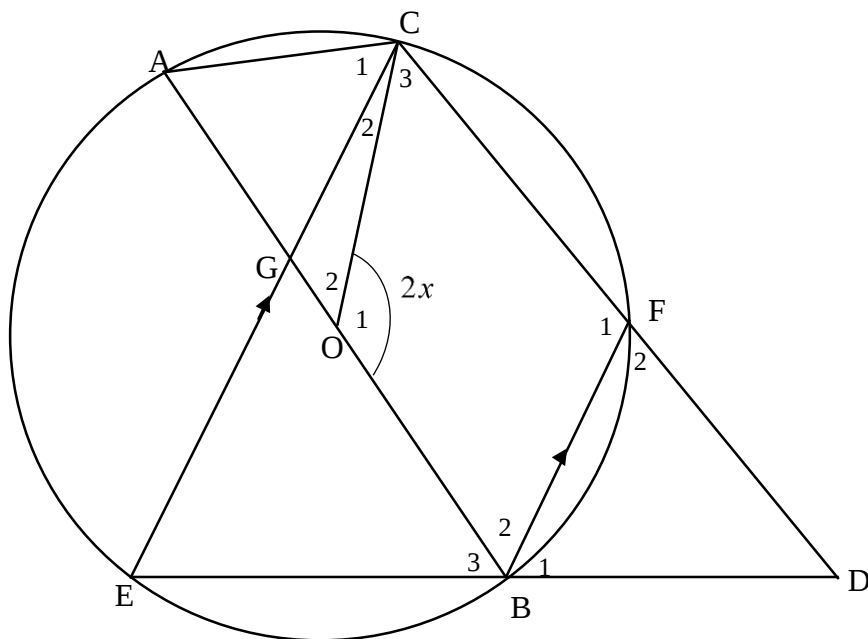
		
7.1	$CR = RD$ (congruency OR SAS) $\hat{CRD} = 180^\circ - 2\beta$ ($\angle$ sin Δ)	✓ $CR = RD$ ✓ answer (2)
7.2	$\hat{TRD} = 90^\circ - \alpha$ $\cos(90^\circ - \alpha) = \frac{h}{RD}$ $RD = \frac{h}{\sin \alpha}$ $CD^2 = \left(\frac{h}{\sin \alpha}\right)^2 + \left(\frac{h}{\sin \alpha}\right)^2 - 2\left(\frac{h}{\sin \alpha}\right)\left(\frac{h}{\sin \alpha}\right)\cos(180^\circ - 2\beta)$ $= \frac{2h^2}{\sin^2 \alpha} - 2\left(\frac{h^2}{\sin^2 \alpha}\right)(-\cos 2\beta)$ $= \frac{2h^2}{\sin^2 \alpha}(1 + \cos 2\beta)$ $= \frac{2h^2}{\sin^2 \alpha}(1 + 2\cos^2 \beta - 1)$ $= \frac{2h^2}{\sin^2 \alpha}(2\cos^2 \beta)$ $= \frac{4h^2}{\sin^2 \alpha}(\cos^2 \beta)$ $\therefore CD = \frac{2h \cdot \cos \beta}{\sin \alpha}$	✓ ratio ✓ $RD = \frac{h}{\sin \alpha}$ ✓ substitution ✓ $\frac{2h^2}{\sin^2 \alpha}(1 + 2\cos^2 \beta - 1)$ ✓ $\frac{4h^2}{\sin^2 \alpha}(\cos^2 \beta)$ (5)
7.3	$CD = \frac{2h \cdot \cos \beta}{\sin \alpha}$	✓ substitution

	$5,4 = \frac{2h \cdot \cos 65^\circ}{\sin 51^\circ}.$ $h = \frac{5,42 \cdot \sin 51^\circ}{2 \cos 65^\circ}.$ $h = 4,96$ $h \approx 5$	$\checkmark h$ to the nearest unit (2)
		[9]

QUESTION 8

8.1		
8.1	$\hat{D}_1 = 33^\circ$ ($\angle$'s in same circle segment)	$\checkmark$ S $\checkmark$ R (2)
8.2	In $\triangle DAE$: $\hat{E}_1 = 90^\circ$ (line from centre to midpt of chord) $\hat{D}_1 = \hat{C} = 33^\circ$ ($\angle$ s in same circle segment) $\therefore \hat{A}_1 = 57^\circ$ ($\angle$'s of $\triangle$) OR In $\triangle EBC$: $\hat{E}_3 = 90^\circ$ (line from centre to midpt of chord) $\hat{C} = 33^\circ$ (given) $\therefore \hat{B}_1 = 57^\circ$ ($\angle$ s of $\triangle$) $\therefore \hat{B}_1 = \hat{A}_1 = 57^\circ$ ($\angle$'s in same circle segment)	$\checkmark$ S $\checkmark$ R $\checkmark$ S (3) $\checkmark$ S $\checkmark$ R $\checkmark$ S (3)
8.3	$\hat{O}_1 = 2\hat{A}_1 = 114^\circ$ ($\angle$ at center = $2 \times \angle$ at circumference)	$\checkmark$ S $\checkmark$ R (2)

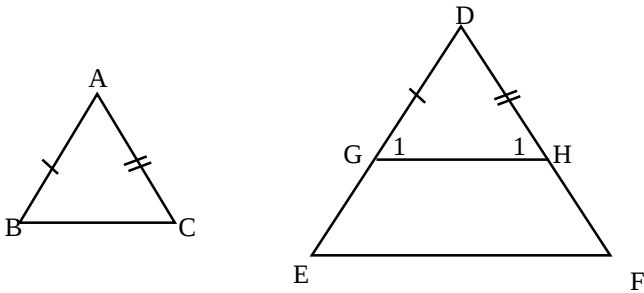
8.4	$\hat{D}_1 + \hat{D}_2 = \hat{A}_1 = 57^\circ$ ($\angle$ s opposite = sides) But $\hat{D}_1 = \hat{C} = 33^\circ$ ($\angle$ s in same circle segment) $\therefore \hat{D}_2 = 24^\circ$ OR $\hat{D}\hat{O}C = 2 \times \hat{B}_1$ ($\angle$ @centre = $2 \times \angle$ @circum) $\hat{D}\hat{O}C = 2 \times 57^\circ$ $= 114^\circ$ $\hat{D}\hat{O}C = \hat{E}_2 + \hat{D}_2$ (ext $\angle$ of Δ) $114^\circ = 90^\circ + \hat{D}_2$ $\therefore \hat{D}_2 = 24^\circ$	$\checkmark$ S/R $\checkmark$ S (2) $\checkmark$ S/R $\checkmark$ S (2)
8.5	$\hat{B}_1 + \hat{B}_2 = 90^\circ$ ($\angle$ in semi-circle) $\hat{A}_2 = 57^\circ$ ($\angle$ s of Δ) OR $\Delta ADE \equiv \Delta ABE$ (S $\angle$ S) $\therefore \hat{A}_1 = \hat{A}_2 = 57^\circ$	$\checkmark$ S $\checkmark$ R $\checkmark$ S (3) $\checkmark$ S $\checkmark$ R $\checkmark$ S (3)
		[12]

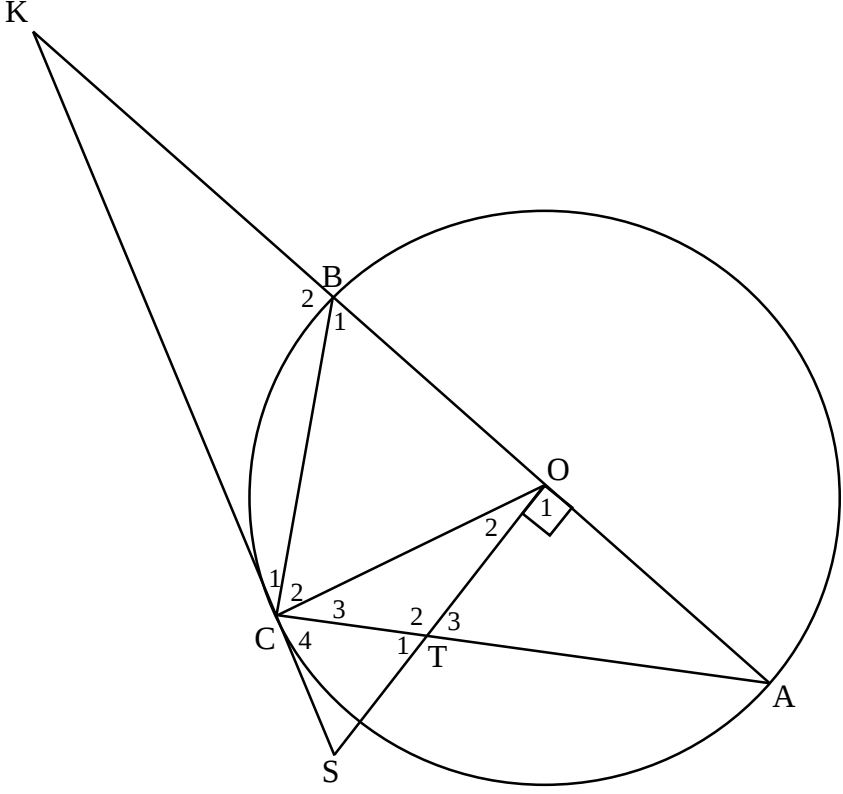
QUESTION 9

9.1	$\hat{E} = x$ ($\angle$ at centre = $2 \times \angle$ at circum) $\hat{F}_1 = 180^\circ - x$ (opposite $\angle$ s of cyclic quad) $\hat{F}_2 = x$ ($\angle$ s on straight line) OR $\hat{E} = x$ ($\angle$ at centre = $2 \times \angle$ at circum) $\hat{F}_2 = x$ (ext $\angle$ of cyclicquad)	$\checkmark$ S $\checkmark$ R $\checkmark$ S (3) $\checkmark$ S $\checkmark$ R $\checkmark$ S/R (3)
9.2	$\hat{F}_2 = x$ (ext $\angle$ of cyclic quad OR straight line) $\hat{B}_1 = x = \hat{E}$ (corresponding $\angle$ s, $EC \parallel BF$) $\therefore \hat{F}_2 = \hat{B}_1 = x$ $\therefore DF = DB$ (sides opposite = $\angle$ s)	$\checkmark$ S $\checkmark$ R $\checkmark$ S $\checkmark$ R (4)

9.3	$\hat{A} = x$ ($\angle$ at centre = $2 \times \angle$ at circum) $\hat{C}_1 + \hat{C}_2 = x$ ($\angle$ s opposite = sides) $\hat{C}_2 + \hat{C}_3 = x$ (ext. $\angle$ of cyclic quad) $\therefore \hat{C}_1 + \hat{C}_2 = \hat{C}_2 + \hat{C}_3$ $\therefore \hat{C}_1 = \hat{C}_3$ OR $\hat{A} = x$ ($\angle$ at centre = $2 \times \angle$ at circum) $\hat{C}_1 + \hat{C}_2 = \hat{A}$ ($\angle$ s opposite = sides) $\hat{A} = \hat{F}_2$ (exterior $\angle$ of cyclic quad) $\hat{F}_2 = \hat{C}_2 + \hat{C}_3$ (corresponding $\angle$ s, CE $\parallel$ BF) $\therefore \hat{C}_1 + \hat{C}_2 = \hat{C}_2 + \hat{C}_3$ $\therefore \hat{C}_1 = \hat{C}_3$	$\checkmark$ S $\checkmark$ S $\checkmark$ S $\checkmark$ R (4) $\checkmark$ S $\checkmark$ R $\checkmark$ S $\checkmark$ R (4)
9.4	CG = FB, CG $\parallel$ BF (given) $\therefore$ CGBF is a parm (one pair opp. sides equal and parallel) BG = FC = 2 (opp. sides of parm.) CF : FD = 2 : 1 $\frac{BD}{ED} = \frac{FD}{CD}$ (line $\parallel$ to one side of Δ or proportionality theorem) $\frac{BD}{ED} = \frac{1}{3}$	$\checkmark$ R $\checkmark$ S/R $\checkmark$ S $\checkmark$ S\R $\checkmark \frac{BD}{ED} = \frac{1}{3}$ (5)
		[16]

QUESTION 10

		
10.1	Construction : $DG = AB$ and $DH = AC$ In $\triangle ABC$ and $\triangle DEF$ 1. $\hat{A} = \hat{D}$ (given) 2. $AB = DG$ (construction) 3. $AC = DH$ (construction) $\therefore \triangle ABC \equiv \triangle DEF$ (SAS) $\therefore \hat{B} = \hat{G}_1$ and $\hat{B} = \hat{E}$ (given) $\therefore \hat{E} = \hat{G}_1$ $\therefore EF \parallel GH$ (corresponding $\angle$s =) $\therefore \frac{DG}{DE} = \frac{DH}{DF}$ (line $\parallel$ to side of $\triangle$) but $AB = DG$ and $AC = DH$ $\therefore \frac{AB}{DE} = \frac{AC}{DF}$	✓ construction ✓ S/R ✓ S ✓ S/R ✓ S ✓ R (6)

10.2		
10.2.1	In $\triangle CKB$ and $\triangle AKC$ $\hat{C}_1 = \hat{A}$ (tan-chord) $\hat{K} = \hat{K}$ (common $\angle$) $\hat{KCT} = \hat{B}_2$ (3^{rd} $\angle$ in Δ) $\therefore \triangle CKB \parallel \triangle AKC$ ($\angle \angle \angle$)	✓S/R ✓S ✓R (3)
10.2.2	$\hat{T}_2 = \hat{O}_1 + \hat{A}$ (ext $\angle$ of Δ) $\hat{KCT} = \hat{C}_1 + \hat{C}_2 + \hat{C}_3$ But $\hat{C}_2 + \hat{C}_3 = 90^\circ$ ($\angle$ s in semi-circle) But $\hat{C}_1 = \hat{A}$ (proven) $\hat{KCT} = \hat{A} + 90^\circ$ $\therefore \hat{T}_2 = \hat{KCT} = \hat{A} + 90^\circ$	✓S/R ✓S ✓R ✓S

		(4)
10.2.3	$\triangle COT \parallel \triangle AKC$ $\hat{TCO} = \hat{A}$ ($\angle$ s opp equal sides; $CO = AO$) $\hat{T}_2 = \hat{KCA}$ (proved) $\hat{O}_2 = \hat{K}$ (3^{rd} $\angle$ in $\triangle$) $\triangle COT \parallel \triangle AKC$ ($\angle \angle \angle$)	$\checkmark$ S/R $\checkmark$ S $\checkmark$ R (3)
10.2.4	$\triangle CKB \parallel \triangle AKC$ $\therefore \frac{BK}{KC} = \frac{CK}{AK}$ $\therefore BK \cdot AK = KC^2$ $\triangle COT \parallel \triangle AKC$ $\therefore \frac{KC}{OT} = \frac{AC}{CT}$ $\therefore KC \cdot CT = AC \cdot OT$ $\therefore KC = \frac{AC \cdot OT}{CT}$ $\therefore KC^2 = \frac{AC^2 \cdot OT^2}{CT^2}$	$\checkmark$ ratio $\checkmark$ S $\checkmark$ ratio $\checkmark$ S (4)
		[20]